

COURSE HANDOUT

Course Code	ACSC13
Course Name	Design and Analysis of Algorithms
Class / Semester	IV SEM
Section	A-SECTION
Name of the Department	CSE-CYBER SECURITY
Employee ID	IARE11023
Employee Name	Dr K RAJENDRA PRASAD
Topic Covered	Single source shortest paths.
Course Outcome/s	Make Use of appropriate tree traversal techniques for finding shortest path
Handout Number	30
Date	8 April, 2023

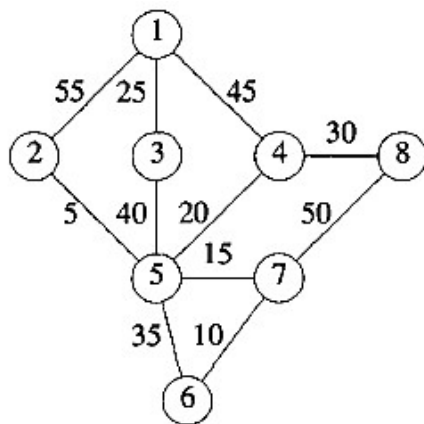
Content about topic covered: Single source shortest path

Single source shortest path

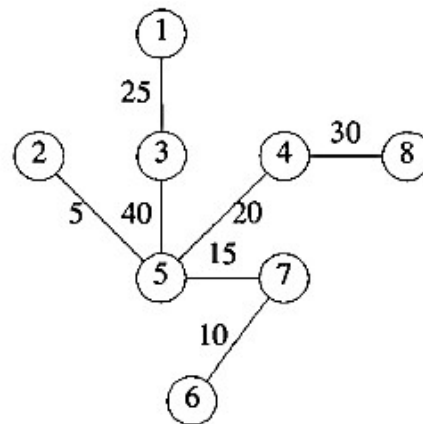
We are given a directed graph $G = (V, E)$, a weighting function cost for the edges of G , and a source vertex V_0 . The problem is to determine the shortest paths from V_0 to all the remaining vertices of G . It is assumed that all the weights are +ve.

```
Algorithm ShortestPaths( $v, cost, dist, n$ )
//  $dist[j]$ ,  $1 \leq j \leq n$ , is set to the length of the shortest
// path from vertex  $v$  to vertex  $j$  in a digraph  $G$  with  $n$ 
// vertices.  $dist[v]$  is set to zero.  $G$  is represented by its
// cost adjacency matrix  $cost[1 : n, 1 : n]$ .
{
    for  $i := 1$  to  $n$  do
    { // Initialize  $S$ .
         $S[i] := \text{false}$ ;  $dist[i] := cost[v, i]$ ;
    }
     $S[v] := \text{true}$ ;  $dist[v] := 0.0$ ; // Put  $v$  in  $S$ .
    for  $num := 2$  to  $n - 1$  do
    {
        // Determine  $n - 1$  paths from  $v$ .
        Choose  $u$  from among those vertices not
        in  $S$  such that  $dist[u]$  is minimum;
         $S[u] := \text{true}$ ; // Put  $u$  in  $S$ .
        for (each  $w$  adjacent to  $u$  with  $S[w] = \text{false}$ ) do
            // Update distances.
            if ( $dist[w] > dist[u] + cost[u, w]$ ) then
                 $dist[w] := dist[u] + cost[u, w]$ ;
    }
}
```

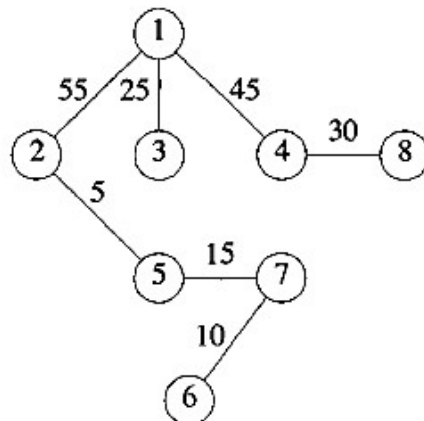
Eg: A graph, minimum cost spanning tree and shortest path spanning tree from vertex 1 are shown below:



(a) A Graph



(b) Minimum cost spanning tree



(c) Shortest path spanning tree from vertex 1.